Annals of Fuzzy Mathematics and Informatics Volume 27, No. 2, (April 2024) pp. 191–204 ISSN: 2093–9310 (print version) ISSN: 2287–6235 (electronic version) http://www.afmi.or.kr https://doi.org/10.30948/afmi.2024.27.2.191



© Research Institute for Basic Science, Wonkwang University http://ribs.wonkwang.ac.kr

# Fuzzy $\alpha$ -b-almost compact space

## Anjana Bhattacharyya

#### Received 16 December 2023; Revised 2 January 2024; Accepted 31 January 2024

ABSTRACT. This paper deals with some applications of fuzzy  $\alpha$ -b-open set. Here we introduce fuzzy  $\alpha$ -b-almost compactness and characterize this concept via fuzzy net and prefilterbase. Also we introduce fuzzy regularly  $\alpha$ -b-open set which characterizes fuzzy  $\alpha$ -b-almost compactness. It is shown that fuzzy  $\alpha$ -b-almost compactness implies fuzzy almost compactness and the converse is true only on fuzzy  $\alpha$ -b-regular space.

### 2020 AMS Classification: 54A40, 03E72

Keywords: Fuzzy  $\alpha$ -b-open set, Fuzzy  $\alpha$ -b-regular space, Fuzzy regularly  $\alpha$ -bclosed set, Fuzzy  $\alpha$ -b-almost compact set (space),  $\alpha$ b-adherent point of a prefilterbase,  $\alpha$ b-cluster point of a fuzzy net.

Corresponding Author: Anjana Bhattacharyya (anjanabhattacharyya@hotmail.com)

## 1. INTRODUCTION

Fuzzy  $\alpha$ -bopen set was introduced in [1] using fuzzy  $\alpha$ -open set as a basic tool. After introducing fuzzy compactness by Chang [2], many mathematicians have engaged themselves to introduce different types of fuzzy compactness. In [3], fuzzy almost compactness was introduced.

In this paper, we introduce the concept of fuzzy  $\alpha$ -*b*-almost compactness which is weaker than fuzzy almost compactness. Here we use fuzzy net [4] and prefilterbase [5] to characterize fuzzy  $\alpha$ -*b*-almost compactness.

In recent time, different types of fuzzy sets, viz., fuzzy soft set and fuzzy octahedron set are introduced and studied. A new branch of fuzzy topology is developed using these types of fuzzy sets. In this context we have to mention [6, 7, 8, 9, 10, 11].

- [3] A. DiConcillio and G. Gerla, Almost compactness in fuzzy topological spaces, Fuzzy Sets and Systems 13 (1984) 187–192.
- [4] Pao Ming Pu and Ying Ming Liu, Fuzzy topology I. Neighbourhood structure of a fuzzy point and Moore-Smith Convergence, J. Math Anal. Appl. 76 (1980) 571–599.
- [5] R. Lowen, Convergence in fuzzy topological spaces, General Topology and Its Applications 10 (1979) 147–160.
- [6] J. G. Lee, G. Senel, P. K. Lim, J. Kim and K. Hur, Octahedron sets, Ann. Fuzzy Math. Inform. 19 (3) (2020) 211–238.
- [7] G. Senel and N. Çağman, Soft closed sets on soft bitopological space, Journal of New Results in Science 3 (5) (2014) 57–66.
- [8] G. Senel and N. Çağman, Soft topological subspaces, Ann. Fuzzy Math.Inform. 10 (4) (2015) 525–535.
- G. Senel, A new approach to Hausdorff space theory via the soft sets, Mathematical Problems in Engineering 1–6. Doi:10.1155/2016/2196743.
- [10] G. Senel, Soft topology generated by L-Soft sets, Journal of New Theory 24 (4) (2018) 88–100.
- [11] G. Senel, J. G. Lee and K. Hur, Distance and similarity measures for octahedron sets and their applications to MCGDM problems, Mathematics 8 (2020) 16–90.
- [12] L. A. Zadeh, Fuzzy Sets, Information and Control 8 (1965) 338–353.
- [13] A. S. Bin Shahna, On fuzzy strong semicontinuity and fuzzy precontinuity, Fuzzy Sets and Systems 44 (1991) 303–308.
- [14] S. Ganguly and S. Saha, A note on compactness in fuzzy setting, Fuzzy Sets and Systems 34 (1990) 117–124.
- [15] M. N. Mukherjee and S. P. Sinha, Almost compact fuzzy sets in fuzzy topological spaces, Fuzzy Sets and Systems 38 (1990) 389–396.

ANJANA BHATTACHARYYA (anjanabhattacharyya@hotmail.com) Department of Mathematics Victoria Institution (College) 78 B, A.P.C. Road Kolkata - 700009, India